## Lesson 2: Identifying Properties of Linear Relations

Warm-Up: Skill question 2 on unit outline

## First Differences

***How do we find out if a relation is going to be linear or not without graphing it? We can use something called "First Differences" to find out. ***

First Differences - Compares the $y$-values to see if a relation is linear or not.
Linear

| Equation | First Differences | Observations |
| :---: | :--- | :--- |
| $y=3 x+2$ |  |  |
| $x$ | $y$ |  |
| -2 |  |  |
| -1 |  |  |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |

## Non-Linear

| Equation | First Differences | Observations |
| :--- | :--- | :--- |
| $y=x^{2}-1$ |  |  |
| $x$ | $y$ |  |
| -2 |  |  |
| -1 |  |  |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |

First Differences

| $x$ | $\boldsymbol{y}$ |
| :---: | :--- |
| -2 | $y_{1}=4$ |
| -1 | $y_{2}=7$ |
| 0 | $y_{3}=10$ |
| 1 | $y_{4}=13$ |
| 2 | $y_{5}=16$ | |  |
| :--- | |  |
| :--- |
| $y_{2}-y_{1}=$ |
| $y_{4}-y_{2}=$ |
| $y_{5}-y_{3}=$ |

## Observations:

1. If the first differences are the same, the relation is $\qquad$ .
2. If the first differences are not the same, the relation is $\qquad$ .

Examples:
Determine whether the following are linear or non-linear:

| $x$ | $y$ |
| :---: | :---: |
| -2 | 3 |
| -1 | 4 |
| 0 | 0 |
| 1 | -2 |


| $x$ | $y$ |
| :---: | :---: |
| -5 | 7 |
| -4 | 4 |
| -3 | 1 |
| -2 | -2 |


| $x$ | $y$ |
| :---: | :---: |
| 0 | -10 |
| 1 | -8 |
| 2 | -7 |
| 3 | -4 |
| 4 | 0 |


| $x$ | $y$ |
| :---: | :---: |
| 4 | 1 |
| 3 | -3 |
| 6 | 9 |
| 5 | 5 |
| 2 | -7 |

