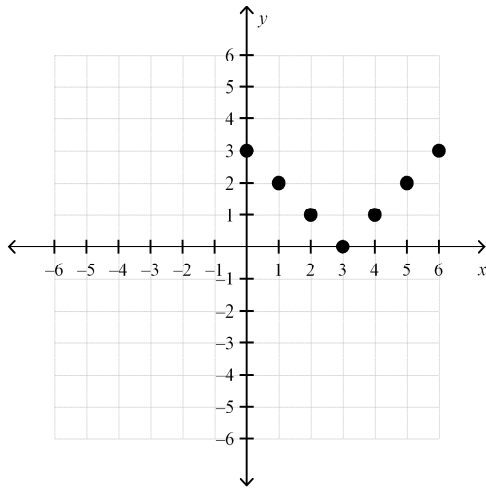


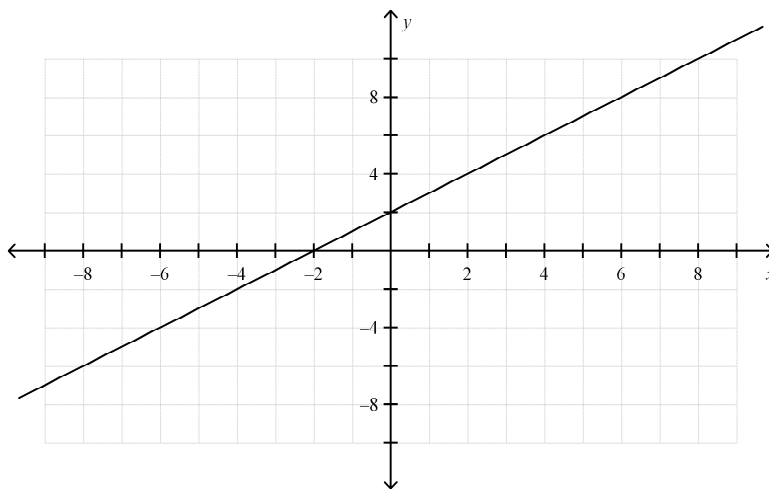
- _____ 44. A skateboard company models its profit with the function $P(x) = -2x^2 + 13x - 15$, where x is the number, in thousands, that the company sells, and $P(x)$ is the profit in tens of thousands of dollars. How many skateboards must the company sell to break even? Use factoring to solve.
- a. at 1500 and 5000 skateboards c. at 1.5 and 5 skateboards
b. at 150 and 500 skateboards d. at 1500 and 50 000 skateboards

Short Answer

45. What are the domain and range of the function?

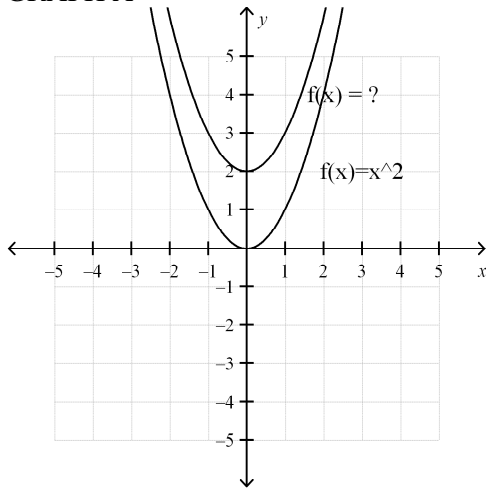


46. The graph of $y = f(x)$ is shown below. Evaluate $f(7)$.

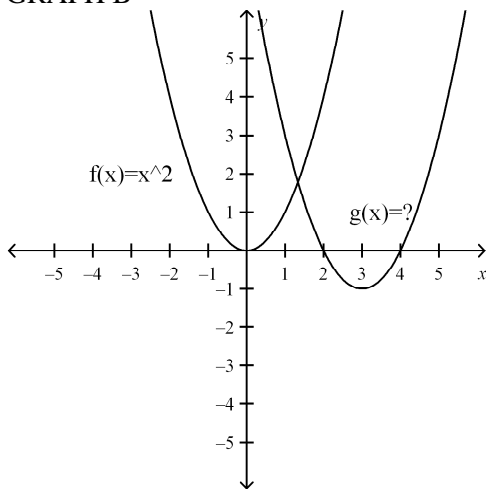


47. Name a function to describe each graph.

GRAPH A



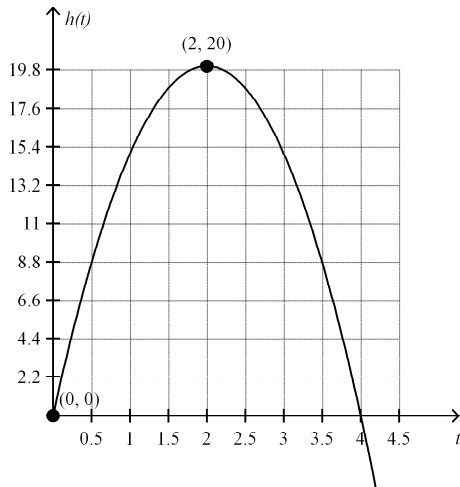
GRAPH B



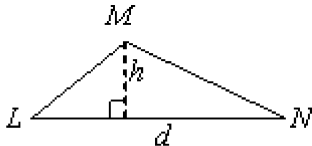
48. What are the domain and range of $h(x) = -(x-2)^2 + 3$?
49. Factor the polynomial fully.
 $-6x^2 - 15x + 9$
50. Factor the polynomial.
 $y^2 - 7y - 30$
51. Draw a rectangle with an area of $x^2 - 9x - 36$. Label the dimensions.
52. Express the quadratic function in standard form.
 $f(x) = -(x-2)(x-4)$
53. For the quadratic function below, determine the coordinates of the vertex without graphing.
 $g(x) = (2x+1)(x-2)$

54. A football is kicked into the air. The height of the football is modelled by $h(t) = -5t^2 + 16t + 1$, where $h(t)$ is the height in metres and t is the time in seconds from its release. When will the football first reach a height of 13 metres?
55. At a craft store, the weekly revenue function for floral wire sold can be modelled with $R(w) = -2w^2 + 20w + 2400$, where both the revenue $R(x)$, and the cost, w , of a roll of floral wire are in dollars. According to the model, what cost will give the maximum revenue?
56. John hits a golf ball into the ocean from a cliff that is 90 metres high. The function $h(t) = -5t^2 + 15t - 90$ gives the approximate height of the golf ball above the water, where $h(t)$ is the height in metres and t is the time in seconds. When will the ball hit the water?
57. Use factoring to solve $-x^2 - x + 12 = 0$. Show your work.
58. Write the factored and standard forms for a quadratic equation with x -intercepts of -5 and -3 and a y -intercept of 1.8 .
59. Does the function $f(x) = -2(x + 6)^2 + 1$ have a maximum or a minimum value? Explain how you decided.
60. Write the function $f(x) = 3(x + 6)^2 - 7$ in standard form.
61. Write the equation of the quadratic function in vertex and standard form whose vertex is at $(-1, 6)$ and that passes through $(2, 24)$.
62. Factor $x^2 - 16x + 64$.
63. Complete the square on $y = x^2 - 16x - 10$.
64. Complete the square on $y = 4x^2 + 24x - 13$.
65. Complete the square to write the function $f(x) = -2x^2 + 5x - 16$ in vertex form. State the vertex.
66. Use the quadratic formula to solve $-8x^2 - 5x + 3 = 0$. Round your answer to two decimal places. If there is no real solution, say so.
67. Use the quadratic formula to solve $12x^2 + 4x + 13 = 0$. Round your answer to two decimal places. If there is no real solution, say so.

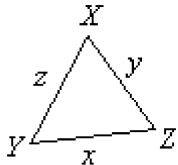
68. The graph shows the height of a football that is kicked for a field goal, where time, t , is in seconds and height, $h(t)$, is in metres. Use the graph to determine an algebraic model.



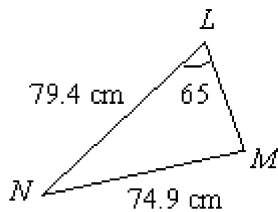
69. A quadratic function has a vertex located at $(2, -8)$ and a y -intercept of -18 . Write the standard form of the quadratic equation.



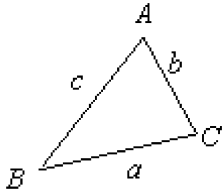
70. If sides \overline{LM} and \overline{MN} of triangle LMN , in the figure above, are 15 cm and 24 cm, respectively, and angles $\angle L$ and $\angle N$ are 49° and 28° , respectively, what is length d ? Round your answer to the nearest centimetre.



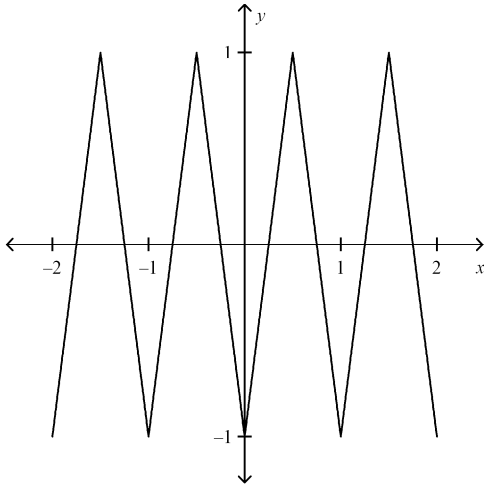
71. Given the figure above, if $\angle Y = 56^\circ$, $\angle Z = 68^\circ$, and $y = 24$ cm, what are the other two sides of triangle XYZ to the nearest tenth of a centimetre?
72. Solve the triangle given below. Round lengths to the nearest tenth of a centimetre and angles to the nearest degree.



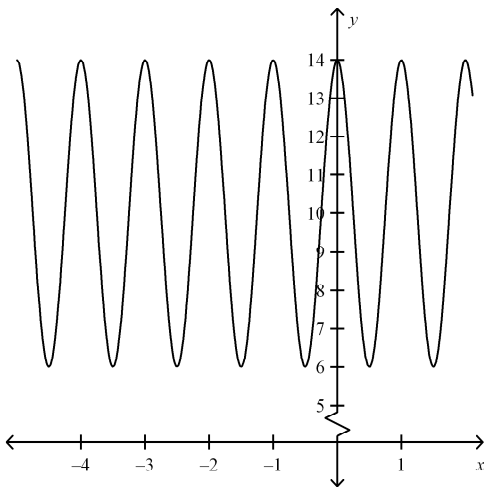
73. Using triangle ABC , if $a = 6.75$ cm, and $c = 7.50$ cm, and $\angle B = 35^\circ$, solve the triangle using the cosine law. Round lengths to the nearest hundredth of a metre and angles to the nearest degree.



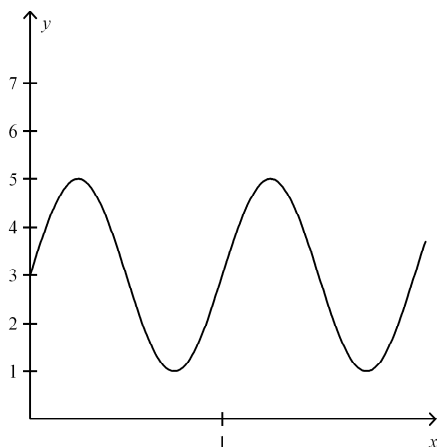
74. What is the period of the function? How many cycles are shown?



75. What is the amplitude of the graph? What is the equation of the axis?



76. Find the amplitude, period and equation of axis of the sinusoidal function.



77. Simplify. Write as a single power: $\frac{(3^4)^3}{3^7(3^2)}$.
78. Simplify: $b^8(b^7)^3$.
79. Simplify, and write as a single power with a positive exponent: $\left(\frac{9}{9^{-3}}\right)^3\left(\frac{9^4}{9^{-2}}\right)$.
80. Simplify and write as a single power with a positive exponent: $\frac{c^{-3}(c^7c^3)^{-1}}{c^{-2}c^8}$.
81. Simplify, and express using positive exponents: $\left((w^{-12})^{-\frac{1}{3}}\right)^{\frac{3}{4}}$.
82. Write $\sqrt[4]{256^3}$ in exponential form.
83. Write $(216)^{\frac{2}{3}}$ in radical form.
84. An antique car was purchased for $\$V_0$ in 1985. It appreciates in value by 2.85% each year. Write an equation that models V , the value of the car, in t years since 1985.
85. A rubber ball is dropped from a height of 10 m. It bounces to a height that is 85% of its previous maximum height after each bounce. After how many bounces will the height of the ball be about 5 m?
86. Light intensity in a lake is reduced by 9% per metre of depth, relative to the light intensity at the surface. What is the light intensity 18 m below the surface of the lake? Round your answer to the nearest hundredth of a percent.
87. Calculate the simple interest due at the end of 30 months if \$10 575 is borrowed at a rate of 3.75%.

88. Gwen wants her investment to be worth \$12 000 in 5 years. The bank will give her 7%/a interest compounded annually. How much does Gwen have to invest now? Round your answer to the nearest cent.
89. Brian took out a loan of \$5500 for his university tuition. How much will he have to pay back at the end of 4 years if the interest on the loan is 7.9%/a compounded semi-annually?
90. Jocelyn wants to build up a fund of \$24 000 over the next 5 years for a down payment on a townhouse. She wants to make regular quarterly deposits into an account that earns 5%/a compounded quarterly. How much should she deposit every 3 months?
91. How much should be deposited into an account to set up an annuity that will provide equal payments of \$140 every 3 months over the next 7 years? The annuity will earn 6.2%/a compounded quarterly.

Problem

92. a) Factor the expression $6x^2 - 4x + 3xy - 2y$.
b) How can grouping the terms in this expression help with factoring?
93. List the five key values of $f(x) = \sin x$ as ordered pairs (x, y) and sketch the function using these points.
94. Sketch a graph of the function $\sin(x - 45^\circ) + 2$.
95. Sketch a graph of the function $f(x) = -2\sin x$.

MCF 3M Practice Exam Answer Section

MULTIPLE CHOICE

1. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 6.6 - More Transformations of sin x: $f(x) = a \sin x$
2. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 6.2 - Periodic Behaviour
3. ANS: B PTS: 1 REF: Knowledge and Understanding
OBJ: 6.6 - More Transformations of sin x: $f(x) = a \sin x$
4. ANS: D PTS: 1 REF: Knowledge and Understanding
OBJ: 7.4 - Working with Rational Exponents
5. ANS: C PTS: 1 REF: Knowledge and Understanding
OBJ: 4.4 - Investigating the Nature of the Roots
6. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 6.4 - Comparing Sinusoidal Functions
7. ANS: D PTS: 1 REF: Knowledge and Understanding
OBJ: 2.3 - Factoring Quadratic Expressions: $x^2 + bx + c$
8. ANS: C PTS: 1 REF: Knowledge and Understanding
OBJ: 7.4 - Working with Rational Exponents
9. ANS: A PTS: 1
10. ANS: C PTS: 1
11. ANS: B PTS: 1 REF: Application
OBJ: 8.3 - Compound Interest: Determining Present Value
12. ANS: B PTS: 1 REF: Application
OBJ: 8.2 - Compound Interest: Determining Future Value
13. ANS: C PTS: 1 REF: Knowledge and Understanding
OBJ: 7.7 - Problems Involving Exponential Decay
14. ANS: D PTS: 1
15. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 6.6 - More Transformations of sin x: $f(x) = a \sin x$
16. ANS: C PTS: 1 REF: Knowledge and Understanding
OBJ: 7.2 - The Laws of Exponents
17. ANS: D PTS: 1 REF: Thinking
OBJ: 8.2 - Compound Interest: Determining Future Value
18. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 4.3 - Solving Quadratic Equations Using the Quadratic Formula
19. ANS: B PTS: 1 REF: Knowledge and Understanding
OBJ: 8.1 - Investigating Interest and Rates of Change
20. ANS: A PTS: 1 REF: Thinking
OBJ: 8.2 - Compound Interest: Determining Future Value
21. ANS: B PTS: 1 REF: Knowledge and Understanding
OBJ: 7.7 - Problems Involving Exponential Decay
22. ANS: B PTS: 1 REF: Knowledge and Understanding
OBJ: 4.2 - Relating the Standard and Vertex Forms: Completing the Square

23. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 7.2 - The Laws of Exponents
24. ANS: A PTS: 1 REF: Communication
OBJ: 7.6 - Solving Problems Involving Exponential Growth
25. ANS: D PTS: 1 REF: Knowledge and Understanding
OBJ: 1.2 - Comparing Rates of Change in Linear and Quadratic Functions
26. ANS: B PTS: 1 REF: Application
OBJ: 8.5 - Regular Annuities: Determining Future Value
27. ANS: D PTS: 1
28. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 1.3 - Working with Function Notation
29. ANS: B PTS: 1 REF: Knowledge and Understanding
OBJ: 7.3 - Working with Integer Exponents
30. ANS: C PTS: 1 REF: Knowledge and Understanding
OBJ: 1.3 - Working with Function Notation
31. ANS: B PTS: 1 REF: Thinking
OBJ: 5.1 - Applying the Primary Trigonometric Ratios
32. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 7.4 - Working with Rational Exponents
33. ANS: D PTS: 1 REF: Knowledge and Understanding
OBJ: 2.5 - Factoring Quadratic Expressions: Special Cases
34. ANS: D PTS: 1 REF: Application
OBJ: 6.3 - Investigating the Sine Function
35. ANS: A PTS: 1 REF: Knowledge and Understanding
OBJ: 1.5 - Graphing Quadratic Functions by Using Transformations
36. ANS: C PTS: 1
37. ANS: D PTS: 1 REF: Thinking
OBJ: 8.2 - Compound Interest: Determining Future Value
38. ANS: B PTS: 1 REF: Thinking
OBJ: 5.1 - Applying the Primary Trigonometric Ratios
39. ANS: B PTS: 1 REF: Application
OBJ: 5.3 - Investigating and Applying the Sine Law in Acute Triangles
40. ANS: B PTS: 1
41. ANS: A PTS: 1 REF: Application
OBJ: 1.1 - The Characteristics of a Function
42. ANS: B PTS: 1 REF: Knowledge and Understanding
OBJ: 1.6 - Using Multiple Transformations to Graph Quadratic Functions
43. ANS: D PTS: 1 REF: Application
OBJ: 3.2 - Relating the Standard and Factored Forms
44. ANS: D PTS: 1 REF: Application
OBJ: 3.5 - Solving Problems Involving Quadratic Functions

SHORT ANSWER

45. ANS:

$$D = \{0, 1, 2, 3, 4, 5, 6\}$$

$$R = \{0, 1, 2, 3\}$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 1.1 - The Characteristics of a Function

46. ANS:

9

PTS: 1 REF: Knowledge and Understanding

OBJ: 1.3 - Working with Function Notation

47. ANS:

Answers may vary. For example:

Graph A: $f(x) = -x^2 + 2$

Graph B: $g(x) = (x - 3)^2 - 1$

PTS: 1 REF: Thinking

OBJ: 1.5 - Graphing Quadratic Functions by Using Transformations

48. ANS:

$$D = \{x \in \mathbf{R}\}$$

$$R = \{y \leq 3 | y \in \mathbf{R}\}$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 1.7 - The Domain and Range of a Quadratic Function

49. ANS:

$$-3(2x - 1)(x + 3)$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 2.2 - Factoring Polynomials: Common Factoring

50. ANS:

$$(y - 10)(y + 3)$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 2.3 - Factoring Quadratic Expressions: $x^2 + bx + c$

51. ANS:

 $x - 12$ $x + 3$

PTS: 1 REF: Communication

OBJ: 2.3 - Factoring Quadratic Expressions: $x^2 + bx + c$

52. ANS:
 $-x^2 + 6x - 8$
- PTS: 1 REF: Knowledge and Understanding
 OBJ: 3.2 - Relating the Standard and Factored Forms
53. ANS:
 $(0.75, -3.125)$
- PTS: 1 REF: Knowledge and Understanding
 OBJ: 3.2 - Relating the Standard and Factored Forms
54. ANS:
 1.2 s
- PTS: 1 REF: Application OBJ: 3.3 - Solving Quadratic Equations by Graphing
55. ANS:
 \$5
- PTS: 1 REF: Application OBJ: 3.4 - Solving Quadratic Equations by Factoring
56. ANS:
 6 s
- PTS: 1 REF: Application OBJ: 3.4 - Solving Quadratic Equations by Factoring
57. ANS:
 $x = -4$ and $x = 3$
 $-(x^2 + x - 12)$
 $-(x - 4)(x + 3)$
- PTS: 1 REF: Knowledge and Understanding
 OBJ: 3.5 - Solving Problems Involving Quadratic Functions
58. ANS:
 $y = 0.12(x + 5)(x + 3)$
 $y = 0.12x^2 + 0.96x + 1.8$
- PTS: 1 REF: Knowledge and Understanding
 OBJ: 3.6 - Creating a Quadratic Model from Data
59. ANS:
 It has a maximum because $a < 0$.
- PTS: 1 REF: Knowledge and Understanding
 OBJ: 4.1 - The Vertex Form of a Quadratic Function
60. ANS:
 $f(x) = 3x^2 + 36x + 101$
- PTS: 1 REF: Knowledge and Understanding
 OBJ: 4.1 - The Vertex Form of a Quadratic Function

61. ANS:

Vertex form: $f(x) = 2(x + 1)^2 + 6$; Standard form: $f(x) = 2x^2 + 4x + 8$

PTS: 1 REF: Knowledge and Understanding

OBJ: 4.1 - The Vertex Form of a Quadratic Function

62. ANS:

$$(x - 8)^2$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 4.2 - Relating the Standard and Vertex Forms: Completing the Square

63. ANS:

$$y = (x - 8)^2 - 74$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 4.2 - Relating the Standard and Vertex Forms: Completing the Square

64. ANS:

$$y = 4(x + 3)^2 - 49$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 4.2 - Relating the Standard and Vertex Forms: Completing the Square

65. ANS:

$$f(x) = -2\left(x - \frac{5}{4}\right)^2 - \frac{103}{8}; \left(\frac{5}{4}, -\frac{103}{8}\right)$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 4.2 - Relating the Standard and Vertex Forms: Completing the Square

66. ANS:

-1 and 0.38

PTS: 1 REF: Knowledge and Understanding

OBJ: 4.3 - Solving Quadratic Equations Using the Quadratic Formula

67. ANS:

no real solution

PTS: 1 REF: Knowledge and Understanding

OBJ: 4.3 - Solving Quadratic Equations Using the Quadratic Formula

68. ANS:

$$h(t) = -5(t - 2)^2 + 20$$

PTS: 1 REF: Application

OBJ: 4.5 - Using Quadratic Function Models to Solve Problems

69. ANS:

$$y = -2.5x^2 + 10x - 18$$

PTS: 1 REF: Knowledge and Understanding

OBJ: 4.6 - Using the Vertex Form to Create Quadratic Function Models from Data

70. ANS:
31 cm
- PTS: 1 REF: Application OBJ: 5.2 - Solving Problems by Using Right-Triangle Models
71. ANS:
 $z = 26.8$ cm
 $x = 24.0$ cm
- PTS: 1 REF: Application
OBJ: 5.3 - Investigating and Applying the Sine Law in Acute Triangles
72. ANS:
 $\angle M = 74^\circ$
 $\angle N = 41^\circ$
 $\overline{LM} = 54.2$ cm
- PTS: 1 REF: Application
OBJ: 5.3 - Investigating and Applying the Sine Law in Acute Triangles
73. ANS:
 $b = 4.34$ cm
 $\angle A = 63^\circ$
 $\angle C = 82^\circ$
- PTS: 1 REF: Application
OBJ: 5.4 - Investigating and Applying the Cosine Law in Acute Triangles
74. ANS:
The period of the function is 1. There are 4 cycles.
- PTS: 1 REF: Application OBJ: 6.2 - Periodic Behaviour
75. ANS:
The amplitude is 4. The equation of the axis is $y = 10$.
- PTS: 1 REF: Thinking OBJ: 6.3 - Investigating the Sine Function
76. ANS:
The amplitude is 2, the period is 1 and the equation of the axis is $y = 3$.
- PTS: 1 REF: Knowledge and Understanding
OBJ: 6.4 - Comparing Sinusoidal Functions
77. ANS:
 3^3
- PTS: 1 REF: Knowledge and Understanding OBJ: 7.2 - The Laws of Exponents
78. ANS:
 b^{29}
- PTS: 1 REF: Knowledge and Understanding OBJ: 7.2 - The Laws of Exponents

79. ANS:
 9^{18}

PTS: 1 REF: Knowledge and Understanding
 OBJ: 7.3 - Working with Integer Exponents

80. ANS:
 $\frac{1}{c^{19}}$

PTS: 1 REF: Knowledge and Understanding
 OBJ: 7.3 - Working with Integer Exponents

81. ANS:
 w^3

PTS: 1 REF: Knowledge and Understanding
 OBJ: 7.4 - Working with Rational Exponents

82. ANS:
 $\frac{3}{256^4}$

PTS: 1 REF: Knowledge and Understanding
 OBJ: 7.4 - Working with Rational Exponents

83. ANS:
 $\sqrt[3]{216^2}$

PTS: 1 REF: Knowledge and Understanding
 OBJ: 7.4 - Working with Rational Exponents

84. ANS:
 $V(t) = V_0(1.0285)^t$

PTS: 1 REF: Communication
 OBJ: 7.6 - Solving Problems Involving Exponential Growth

85. ANS:
 4 bounces

PTS: 1 REF: Thinking OBJ: 7.7 - Problems Involving Exponential Decay

86. ANS:
 18.31%

PTS: 1 REF: Application OBJ: 7.7 - Problems Involving Exponential Decay

87. ANS:
 \$991.41

PTS: 1 REF: Knowledge and Understanding
 OBJ: 8.1 - Investigating Interest and Rates of Change

88. ANS:
\$8555.83

PTS: 1 REF: Application OBJ: 8.2 - Compound Interest: Determining Future Value

89. ANS:
\$7498.23

PTS: 1 REF: Application OBJ: 8.2 - Compound Interest: Determining Future Value

90. ANS:
\$1063.69

PTS: 1 REF: Application OBJ: 8.5 - Regular Annuities: Determining Future Value

91. ANS:
\$3160.63

PTS: 1 REF: Knowledge and Understanding
OBJ: 8.6 - Regular Annuities: Determining Present Value

PROBLEM

92. ANS:

a) $6x^2 - 4x + 3xy - 2y$

$$(6x^2 - 4x) + (3xy - 2y)$$

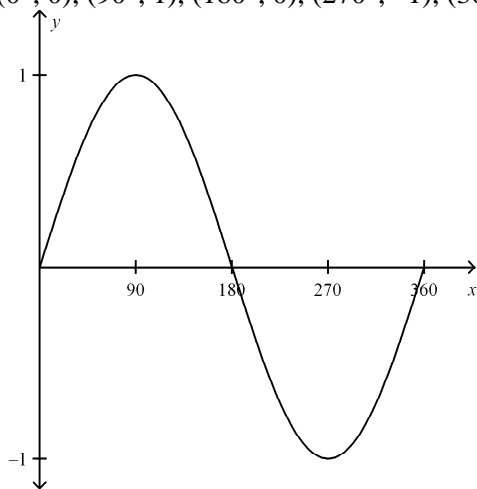
$$2x(3x - 2) + y(3x - 2)$$

$$(3x - 2)(2x + y)$$

b) Grouping the terms will allow you to see the common factor.

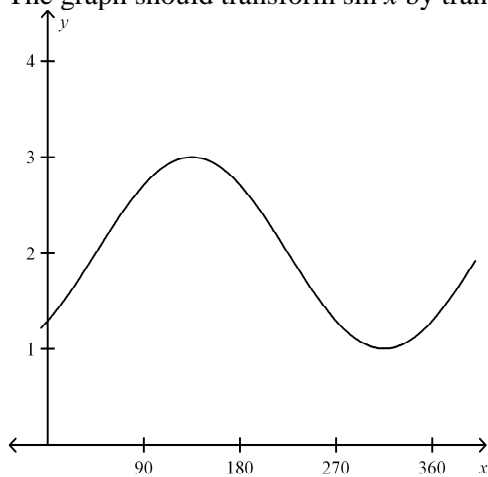
PTS: 1 REF: Communication
OBJ: 2.2 - Factoring Polynomials: Common Factoring

93. ANS:
 $(0^\circ, 0), (90^\circ, 1), (180^\circ, 0), (270^\circ, -1), (360^\circ, 0)$



PTS: 1 REF: Thinking OBJ: 6.3 - Investigating the Sine Function

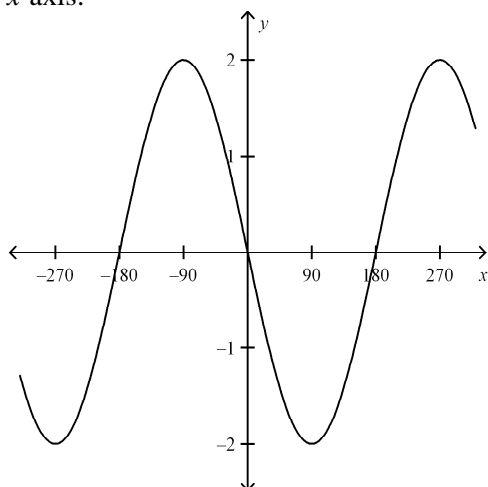
94. ANS:
 The graph should transform $\sin x$ by translating up 2 units and to the right 45° .



PTS: 1 REF: Thinking
 OBJ: 6.5 - Transformations of the Sine Function: $f(x) = \sin(x - c)$ and $f(x) = \sin x + d$

95. ANS:

The graph retains the same x -intercepts as $\sin x$, but the amplitude is 2 and the function is reflected over the x -axis.



PTS: 1

REF: Thinking

OBJ: 6.6 - More Transformations of $\sin x$: $f(x) = a \sin x$